Optimal Charging Schemes for Electric Vehicles in Smart Grid: A Contract Theoretic Approach

Ke Zhang[®], Yuming Mao, Supeng Leng[®], *Member, IEEE*, Yejun He[®], *Senior Member, IEEE*, Sabita Maharjan[®], *Member, IEEE*, Stein Gjessing, *Member, IEEE*, Yan Zhang, *Senior Member, IEEE*, and Danny H. K. Tsang[®], *Fellow, IEEE*

Abstract-Due to their environment friendliness, electric vehicles (EVs) are anticipated to form a considerable fraction of vehicles for transportation in smart cities. It is essential to design an electricity charging scheme that takes the utilities of both the charging stations and the EVs into consideration. However, the self-interested nature of the EVs together with the information asymmetry between the energy demand and supply sides makes the design a significant challenge. In this paper, we propose a queuing network-based model to characterize the charging process of the multiple EVs in a renewable energy-aided charging station. Based on the model, we adopt a contract theoretic approach to design an optimal charging policy in an information asymmetry scenario. Furthermore, we propose the new contract-based charging rate assignment and admission control schemes that maximize the utility of the charging station under certain charging constraints. To derive the optimal contract, we present a two-step iterative algorithm and prove its convergence. We evaluate the proposed schemes based on the IEEE 69-bus distribution test system. Results indicate that the contract-based charging schemes can effectively benefit both the charging stations and the EVs and concurrently improve the load level of the smart grid.

Manuscript received May 17, 2017; revised December 16, 2017 and March 31, 2018; accepted May 13, 2018. Date of publication August 7, 2018; date of current version September 7, 2018. This work was supported in part by the programs of NSFC under Grant 61374189, Grant 61422201, Grant 61370159, Grant 61372077, Grant U1301255, and Grant U1501251, in part by the Science and Technology Program of Guangdong Province under Grant 2015B010129001 and Grant 2016B090918080, in part by the Special-Support Project of Guangdong Province under Grant 2014TQ01X100, in part by the High Education Excellent Young Teacher Program of Guangdong Province under Grant YQ2013057, in part by the Science and Technology Program of Guangzhou under Grant 2014J2200097 (Zhujiang New Star Program) and Grant 201707010490, in part by the Research Council of Norway under Project 240079/F20, and in part by the Fundamental Research Funds for the Central Universities, China, under Grant 2672018ZYGX2018J001. The Associate Editor for this paper was C. Sommer. (Corresponding author: Yan Zhang.

K. Zhang, Y. Mao, and S. Leng are with the School of Information and Communication Engineering, University of Electronic Science and Technology of China, Chengdu 611731, China (e-mail: zhangke@uestc.edu.cn; ymmao@uestc.edu.cn; spleng@uestc.edu.cn).

Y. He is with the College of Information Engineering, Shenzhen University, Shenzhen 518060, China (e-mail: heyejun@126.com).

S. Maharjan is with the Simula Metropolitan Center for Digital Engineering, 1364 Fornebu, Norway, and also with the Department of Informatics, University of Oslo, 0315 Oslo, Norway (e-mail: sabita@simula.no).

S. Gjessing and Y. Zhang are with the Department of Informatics, University of Oslo, 0315 Oslo, Norway (e-mail: steing@ifi.uio.no; yanzhang@ieee.org).

D. H. K. Tsang is with the Department of Electronic and Computer Engineering, The Hong Kong University of Science and Technology, Hong Kong (e-mail: eetsang@ece.ust.hk).

Color versions of one or more of the figures in this paper are available online at http://ieeexplore.ieee.org.

Digital Object Identifier 10.1109/TITS.2018.2841965

Index Terms—Electric vehicle, charging scheme, queuing model, contract theory, admission control.

I. INTRODUCTION

BEING a paradigm of green transportation, Electric Vehicles (EVs) form one of the main components for sustainable smart cities [1]. In order to enhance the energy efficiency of the grid as well as provide reliable operation of EVs, it is of paramount importance to study the characteristics and control policies of EVs charging. In recent years, vehicle platoons have gained increasing attention with innovative capabilities for dealing with traffic congestion and improving energy efficiency. Some research and demonstration have been taken on the application of vehicle platoons [2]. An EV platoon is a group of EVs composed of a head vehicle and a number of followers traveling the same route [3]. As an EV platoon always arrives collectively at a charging station, the feature of the arriving EV platoons challenges the charging service policy of the stations, which is always designed for the independently arriving EVs. Moreover, the EVs charging scheduling schemes should consider the Quality of Service (QoS) which can be characterized by the charging rates, the electricity price and the waiting time. Nonetheless, uncoordinated charging of a high number of EVs may significantly increase burden on the local neighborhood circuits of the grid [4]. Thus, an efficient charging policy should consider both the constraints of the grid and customer satisfaction.

Intuitively, the willingness of the EVs to coordinate in the charging process may be of great importance to the viability of an optimal charging service. However, in practice, EVs are self-interested. It is unrealistic to assume that they follow the control instructions from the charging station unconditionally. In addition, there may exist information asymmetry between the charging station and the EVs which is caused by the station's unawareness of the actual charging preference of the EVs. These factors pose a significant challenge on designing the optimal charging scheme.

A contract theoretic approach is a powerful tool from microeconomics that brings two self-interested and rational entities to agreements by providing economic incentives [5]. In this paper, we design an EV charging mechanism which maximizes the utility of the charging station and concurrently enhances the QoS of the charging process. To the best of our knowledge, this is the first work that applies contract theoretic approach in arranging power resources of charging stations for

1524-9050 © 2018 IEEE. Personal use is permitted, but republication/redistribution requires IEEE permission. See http://www.ieee.org/publications_standards/publications/rights/index.html for more information.

serving EV platoons. In addition, unlike traditional contractbased strategies, which mainly focus on contract adjustment to improve service performance, we combine contract design with service QoS requirement and propose optimal contracts incorporating charging admission control policies. The main contributions of this paper are as follows:

- We introduce a contract theoretic approach for resource management at charging stations that serve EV platoons. In order to maximize the utilities of the charging stations while also satisfying certain charging QoS constraints, we incorporate EV platoon admission control into charging contract design.
- To cope with the variable characteristics of different charging operation scenarios, we propose an efficient two-step iterative algorithm to obtain the optimal contract and prove the algorithms convergence.
- We present a queuing network based performance analysis framework for the charging process of EV platoons served at a renewable aided charging station. Moreover, by implementing the proposed contract-based charging schemes into charging process management, we obtain the steady-state distribution of the queuing network.

The rest of the paper is organized as follows. In Section II, we review related work. A platoon-based charging queuing model and the problem formulation are derived in Section III. The contract-based charging rates assignment and admission control schemes are described in Section IV. In Section V, we derive the steady-state distribution of the charging queuing system. Performance evaluation is presented in Section VI. Finally, we conclude our work in Section VII.

II. RELATED WORK

EV platoon is a promising transportation way with significant environmental and safety benefits. There are several projects and experiments focusing on demonstrating platoon in general or the EV platoon. For instance, the SARTRE project investigates and trials technologies for platoon driving of road vehicles [6]. In [7], experimental results have shown that platooning of trucks improves vehicle energy efficiency. Several practical experiments have also been conducted on real EV platoons. For instance, the autonomous platoon driving system was tested in the experiment shown in [8]. The performance of the platooning control scheme designed for urban electric vehicles was investigated via full-scale experiments. Furthermore, some studies have carried out on the EV platoons. For example, Yu *et al.* [9] proposed a predictive control system for Hybrid Electric Vehicle (HEV) platoons.

As battery charging technologies play a critical role in the support and proliferation of EVs, EVs' charging systems have been extensively studied. Wang *et al.* [10] presented a comprehensive overview of coordinated EV charging mechanism from an algorithmic perspective. The study in [11] focused on the spatial-temporal random dynamics of EVs, and proposed a probabilistic model for charging demands of moving EVs. Tang and Zhang [12] formulated optimal EV charging scheduling as a finite-horizon dynamic programming, and presented a low complexity online algorithm to solve the program. The work in [13] studied the charging schemes for

large populations of EVs, and provided a hierarchical charging control framework. Coping with the growth of wind power generation, He et al. [14] designed a bi-layer optimization scheduling of generators, electric vehicles as well as wind power in the two dimensions of time and space. Aiming to establish an optimal load pattern, Alonso et al. [15] introduced a genetic algorithm based scheme, which coordinates electric vehicle charging with various characteristics of the smart grid. Through a hierarchical game approach, Tan and Wang [16] proposed a charging navigation framework for electric vehicles, where both power system and transportation system were considered. Saad et al. [17] gave an overview of applying game-theoretic methods in managing microgrid systems, power demand response coordination and smart grid communications. Rigas et al. [18] focused on the utilization of artificial intelligence in managing electric vehicles in smart grid, including elaboration of challenges and comparison of technical approaches.

The queuing theory is a powerful mathematical tool to construct the model of an operation system. Through this model, some statistical characteristics, such as queue lengths and waiting time, can be obtained. These characteristics are very helpful to improve the design of the system operation schemes. We note that a few recent studies have adopted queuing theory to study the charging process and improved the quality of charging service. For example, in [19], the queuing theory was adopted to model the EV aggregation behavior. In [20], the capacity of an EV charging station was determined through a queuing theoretic approach. In [21], the process of charging multiple EVs at a charging facility was modeled as a queuing network. Based on the proposed queuing model for battery swapping stations, Tan et al. [22] and Sun et al. [23] introduced some valuable performance indicators of the charging system, and presented an optimal charging scheme by dynamic programming. The work in [24] modeled fast charging as a queuing system where both the direct current fast charging model and the revenue model of the station are incorporated into the queuing analysis. However, none of the aforementioned work has considered the influence of EV platoons charging in the stations.

Due to their suitability for modeling market mechanisms of electricity trading, economic theories have now been pervasively and successfully applied in the studies of smart grid. For instance, Zeng *et al.* [25] used group selling based auction for motivating EVs to feedback power to the grid. The studies in [26] proposed a deadline differentiated pricing scheme, which incentivizes charging EVs to defer their electric power consumption. Shuai *et al.* [27] focused on economic and incentive aspects of electric vehicle charging process, and provided a comprehensive survey of charging economic models as well as charging management schemes.

Being a promising economic theoretic approach, contract theory is widely used in various resource management problems. For instance, Duan *et al.* [28] investigated cooperative spectrum sharing under incomplete information, and proposed contract-based optimal sharing schemes between primary and secondary users. In [29], contract theory was adopted to address the problem of relay selection in OFDM-based wireless systems. To mitigate the interference between remote radio heads and macro base stations, Peng et al. [30] introduced a contract-based interference coordination framework. Asheralieva and Miyanaga [31] focused on joint user association and inter-cell interference mitigation in heterogeneous LTE-A networks, and proposed an efficient contract-based mechanism. Applying contract theory in the field of power management, Gao et al. [32] proposed a contract-based mechanism which is helpful in matching the aggregated energy rate to the service request while also maximizing the EVs' profits. Namerikawa et al. [33] utilized a real time pricing contract to guarantee the participation of the energy suppliers and consumers in the energy market. To improve power transmission efficiency, Zhang et al. [34] proposed an energy exchange mechanism between electric vehicles, where the energy trading process was modeled and managed in a contract theoretic approach. Nevertheless, most of these studies only considered the quantity of the required energy and the profits gained by both sides. Few studies of them have taken into account the QoS of the charging process in the energy exchange.

Serving as an important means of transportation in the modern society, EVs are expected to have short charging duration. There are a few studies focused on the charging scheme with charging duration limitations. For example, Xu et al. [35] formulated the EV charging scheduling problem as a Markov decision process, where both the charging task deadlines and the random electricity cost have been considered. Yu et al. [36] proposed an intelligent energy management system with charging deadline constraints and energy source choices. You et al. [37] proposed a cooperative charging scheme for a charging station, which enables EVs to economically be charged within the given deadlines. Zhou et al. [38] formulated an EV charging optimization problem to minimize the supply costs of charging stations, which takes into account the individual charging deadline constraint of each EV. However, none of these works have incorporated the charging QoS guarantee strategies into the economic schemes.

Different from these studies, in this paper we concentrate on the charging process of EV platoons and propose the optimal contract-based charging schemes to improve the utilities of the charging station while guarantee the charging QoS.

III. SYSTEM MODEL AND PROBLEM FORMULATION

Fig. 1 shows a renewable energy aided charging station with a total of *c* parallel chargers. The charging station is modeled as a queuing network, where the input is the platoons needing electrical power charging and the output is the fully charged platoons. We consider that the arrival of the EV platoons follows a Poisson process with arrival rate λ_p [22]. In practice, the Poisson arrival model of vehicles on highways has been verified in [39]. As vehicle platoons have not been widely used in our real life, there is scarcely any statistical data for modeling the arriving platoons. For an EV platoon, a group of EVs may travel together in the same route, and we can take each platoon as a special EV. Thus, it is not exceptional to assume that the arrival process for EV platoons follows a Poisson process.



Fig. 1. EV platoons charging at a renewable energy supplied station.

The maximum capacity of the charging station for accommodating vehicles is limited to N, i.e., besides the c charging vehicles the station can at most provide N - c parking lots. The size of each platoon is a random variable denoted as z. The probability that a platoon consists of z vehicles is denoted as $P_{l,z}$, where $\sum_{z=1}^{Z_{\text{max}}} P_{l,z} = 1$. We consider EV platoons charging fairly with the first-come-first-serve policy. The State of Charge (SoC) of each arriving EV follows an i.i.d. random variable.

The energy charging schedules of the platoons and the charging station are considered to operate in a discrete time model with fixed length time slots. For ease of analysis, we consider that the length of each time slot, denoted as τ , is short, and that no more than one platoon arrives at the station during one time slot. Let time slot *t* denote the time interval $(t\tau, (t+1)\tau], t = \{0, 1, 2, ...\}$.

Let $P_e(e(t) = m)$ denote the probability that the renewable energy source e(t) generates m units of electricity in time slot t, $m \ge 0$. Here, one unit is defined as the average energy consumed for charging one EV. The generated renewable energy is divided into two parts. The first part is imported into the station for the charging service, and the remaining part is sold to the grid. As each time slot is a short time interval, the number of EVs in the charging station at time slot t + 1mainly depends on that at time slot t. The charging demand from the EVs changes slightly between these two consecutive slots, especially in the charging station at a steady state. Thus, we can predict the charging demand of each time slot based on that of the last slot. We consider that for each time slot, the amount of the imported renewable energy depends on the charging demand of the EVs. Then, the imported renewable energy in time slot t + 1 is defined as

$$r_{re}(t+1) = \min\{e(t+1), s(t), M\},\tag{1}$$

TABLE I MAIN ABBREVIATIONS AND NOTATIONS

Symbol	Description
EV	Electric Vehicle
HEV	Hybrid Electric Vehicle
SoC	State of Charge
LUIC	Local Upward Incentive Constraint
LDIC	Local Downward Incentive Constraint
c	Number of parallel chargers
N	Maximum capacity of the charging station
z	Size of each EV platoon
$P_{l,z}$	Probability of a platoon has $z \in Vs$
τ	Length of each time slot
λ_n	Poisson arrival rate of EV platoons
e(t)	Renewable energy generated in time slot t
m	Amount of renewable energy
s(t)	Number of EVs served in time slot t
	Limitation of the renewable energy transmis-
M	sion capacity
G	Types of EV platoons
θ	Willingness-to-pay parameter of EV platoons
$P_{r,i}$	Probability of a platoon belonging to type- θ_i
U_n	Charging utility of a platoon
v	Evaluation of a charging platoon
q	Payment for a charging platoon
$\hat{T}_{\theta,i}$	Waiting tolerance threshold of type- θ_i platoon
r_i	Charging rate for type- θ_i platoon
ξ	Unit charging rate cost for the charging station
d	Electrical energy demand of the district
U_{sta}	Expected utility of the charging station
$P_{ac.i}$	Admission policy of type- θ_i platoons
$P_{loss,i}$	Probability of type- θ_i platoon's service loss
ε	QoS threshold of service loss
L	Number of EVs in the charging station
μ_i	Average charging time for type- θ_i platoons
w	Waiting time of EV platoons
Ŧ	Average service time for a charger to finish
t	charging one EV
s	Number of served EVs during last time slot
i, b	Amount of imported renewable energy
n,m	Number of EVs in the charging system
0	Probability of z new EV arrivals at the charg-
ρ_z	ing station during a time slot
$\varpi, \rho_0, \alpha_1, \alpha_2$	coefficients

where s(t) is the number of EVs that have been served by the station in time slot $t, s(t) \ge 0$. Due to the definition of the unit of the renewable energy, the amount of consumed energy in time slot t is numerically equal to s(t). M is the limitation of the energy transmission capacity of the line connecting the renewable generator and chargers in one time slot.

We consider there are *G* types of EV platoons according to their preferred charging rates, with different willingnessto-pay parameters of $\theta_1, \theta_2, \ldots, \theta_G$ [32], [40]. Here, charging rate indicates the amount of electrical energy supplied by the charging station to the EV platoons per unit of time. The charging preference type is private information of each platoon which is not known to the charging station. However, we assume that the charging station has the knowledge of the probability distribution of platoon types based on statistical information. The probability of the EV platoons belonging to type- θ_i is denoted as $P_{r,i}$ with $\sum_{i=1}^{G} P_{r,i} = 1$. Without loss of generality, we consider that $\theta_1 < \theta_2 < \ldots < \theta_G$ and the higher θ implies higher preference for faster charging. The utility of a type- θ platoon which charges at rate *r* can be expressed as

$$U_p(\theta, r, q) = v(\theta, r) - q, \qquad (2)$$

where q is the cost a platoon pays for choosing charging rate r. $v(\theta, r)$ is the evaluation function of a platoon according to the archived charging rate, defined as $v(\theta, r) = \varpi log(1+\theta r)$, $r \in \mathbb{R}^+$. Here ϖ is a coefficient with the same unit as q. For analysis simplicity, the value of ϖ is set to 1. In practical charging operations, the evaluation function should satisfy two properties [41]. First, a driver obtains more utility when the driver's EV served with faster charging rate, especially for the driver of the higher θ type EVs. Second, the EV drivers may have less interest to charge when the charging rate increases. Logarithmic function is one of the functions that satisfy these two properties. Due to its properties and mathematical simplicity, logarithmic function utility has been widely used in many different fields [42]-[44]. In our paper, we also adopt the logarithmic representation in the evaluation function. It is noteworthy that any increasing concave function can be used as the evaluation function, and the change of these functions does not affect the design of the charging schemes.

Besides the charging rate cost, another critical issue in the charging system is the charging QoS. In this paper, we mainly focus on the study of the service loss caused by impatient drivers waiting in the queue for a certain length of time, and propose an admission control scheme for the arriving platoons to reduce the service loss probability. We assume that the platoons of type- θ will leave the charging station if they are kept waiting for longer than T_{θ} . As long as a platoon has an overview of the battery status of its vehicles, it can drive to an alternative and feasible charging station where it will have to wait for less time, or wait at the current station and charge at a slower rate if the remaining power is insufficient to drive to the alternative stations. For these platoons that reduce their charging rate requirements due to the unavailability of alternative stations, we can model them as new types of platoons with reduced charging rates and different willingnessto-pay parameters. It is noteworthy that our contract-based approach can be directly applied even with the additional types of platoons. Recall that a larger θ means higher charging rate preference, which in turn implies less tolerance on waiting. Thus we can get $T_{\theta,1} > T_{\theta,2} > \ldots > T_{\theta,G}$. We assume that the charging station could provide G different charging rates $\{r_1, r_2, \ldots, r_G\}$, whose charging times are exponentially distributed due to the different initial EV battery's SoC.

The charging station should pay cost to the grid for the energy it consumes, which is affected by two factors. The first one is the renewable energy imported into the charging station. The other factor is the load of the power grid. In smart grid, the load level information can be delivered to each charging station through cable or wireless communications. Thus, the unit charging rate cost for the station is defined as

$$\xi = \rho_0 - \alpha_1 r_{re}(t) + \alpha_2 (\frac{d}{d_{ideal}})^{\gamma}, \qquad (3)$$

where ρ_0 is the base cost of unit charging rate. α_1 , α_2 are coefficients, and γ is a constant, $\gamma > 1$. *d* is the electrical

energy demand of the district where the charging station is located excluding the charging consumption. d_{ideal} is the optimal demand of the district set by the power grid company. Typically, d_{ideal} is set as 80% of the nominal capacity of the transformer in a district [45].

In order to improve the revenue obtained by the charging station and the charging QoS while ensuring that each EV platoon can obtain the best match charging rate according to its type, we propose an optimization problem incorporated with charging rates assignment and charging admission control, which is formulated as

$$\max_{\{q_{i}, r_{i}, P_{ac,i}\}} U_{sta} = \sum_{i=1}^{G} (1 - P_{loss,i}) P_{ac,i} P_{r,i} (q_{i} - r_{i}\xi)$$
s.t. C1: $v(\theta_{i}, r_{i}) - q_{i} \ge v(\theta_{i}, r_{j}) - q_{j}, \quad i \ne j,$
C2: $v(\theta_{i}, r_{i}) - q_{i} \ge 0, \quad r_{\min} \le r_{i} \le r_{\max},$
C3: $q_{i} \ge 0, \quad P_{loss,i} \le \varepsilon, \quad P_{ac,i} = \{0, 1\}, \quad i, j \in \mathcal{G}.$
(4)

In (4), U_{sta} is the expected utility of the charging station. $P_{loss,i}$ is type- θ_i platoon service loss probability due to long waiting time. $P_{ac,i}$ is the admission policy of type- θ_i platoons, where the policy is either "always reject" with $P_{ac,i} = 0$ or "always accept" with $P_{ac,i} = 1$. U_{sta} can be maximized through optimizing the design of charging rates $\{r_i\}$ and corresponding costs $\{q_i\}$ as well as the admission policy set $\{P_{ac,i}\}$ for each type of platoons. In C2, r_{min} and r_{max} are constants, which are the limitation of the charging rate of each charger in practice. ε in C3 is a constant QoS threshold, and $\mathcal{G} = \{1, 2, \ldots, G\}$. Constraint C1 in (4) is nonlinear which makes the solution of the optimization problem challenging.

IV. CONTRACT-BASED CHARGING RATE ASSIGNMENT AND ADMISSION CONTROL

In this section, we model the charging rate assignment and admission control schemes as a contract problem. Based on the analysis of the relation between the admission control policies and the assigned charging rates, a two-step iterative algorithm to obtain the optimal solution of the problem is presented.

A. Feasible Contracts Formulation

The charging station effectively specifies a rate-cost bundle contract denoted as (r_i, q_i) for type- θ_i platoons, $i \in \mathcal{G}$. To ensure its feasibility, the contract should satisfy both the Individual Rational (IR) constraint and the Incentive Compatibility (IC) constraint. In the considered problem, the IR constraint could be denoted as $U_p^i = v(\theta_i, r_i) - q_i \ge 0$, $i \in \mathcal{G}$, which motivates the participation of the self-interested EV platoons. Due to the IR constraint, if the type- θ_i platoons are prohibited by the admission control policy, i.e., $P_{ac,i} = 0$, correspondingly, the charging cost q_i of contract $\{r_i, q_i\}$ could be set to a sufficiently large number. The IC constraint makes the platoons of type- θ_i prefer the contract (r_i, q_i) over all other options, i.e., $v(\theta_i, r_i) - q_i \ge v(\theta_i, r_j) - q_j$, $i, j \in \mathcal{G}$, $i \neq j$. Considering the feasibility of the contracts, the optimization problem (4) can be rewritten as

$$\max_{\{q_i, r_i, P_{ac,i}\}} U_{sta} = \sum_{i=1}^{G} (1 - P_{loss,i}) P_{ac,i} P_{r,i} (q_i - r_i \xi)$$

s.t. C1: $v(\theta_1, r_1) - q_1 \ge 0$,
C2: $v(\theta_i, r_i) - q_i \ge v(\theta_i, r_{i+1}) - q_{i+1}, \ 1 \le i < G$,
C3: $v(\theta_i, r_i) - q_i \ge v(\theta_i, r_{i-1}) - q_{i-1}, \ 1 < i \le G$,
C4: $r_{\min} \le r_1 \le r_2 \le \ldots \le r_G \le r_{\max}$,
C5: $q_i \ge 0$, $P_{loss,i} \le \varepsilon$, $P_{ac,i} = \{0, 1\}, \ i \in \mathcal{G}$.
(5)

In (5), constraints C2 and C3 are called Local Upward Incentive Constraint (LUIC) and Local Downward Incentive Constraint (LDIC), respectively [5].

B. Optimal Contract Simplification

The maximum utility of the charging station will be obtained under the condition that LDICs are binding for the optimization problem. Given the monotonicity condition $r_{i-1} < r_i$, $1 < i \le G$, and that all the LDICs are binding, then the LUICs can be drawn from the LDICs [5]. Thus, we can say that with the monotonicity condition and binding LDICs, LUICs could be reduced. Then, the optimization problem in (5) can be simplified as

$$\max_{\{q_i, r_i, P_{ac,i}\}} U_{sta} = \sum_{i=1}^{G} (1 - P_{loss,i}) P_{ac,i} P_{r,i} (q_i - r_i \xi)$$

s.t. C1: $v(\theta_1, r_1) - q_1 = 0$,
C2: $v(\theta_i, r_i) - q_i = v(\theta_i, r_{i-1}) - q_{i-1}, \quad 1 < i \le G$,
C3: $r_{\min} \le r_1 \le r_2 \le \ldots \le r_G \le r_{\max}$,
C4: $q_i \ge 0, \quad P_{loss,i} \le \varepsilon, \quad P_{ac,i} = \{0, 1\}, \quad i \in \mathcal{G}.$
(6)

Here, we define the notations $\Delta_1 = 0$, and $\Delta_i = v(\theta_i, r_i) - v(\theta_i, r_{i-1})$, $1 < i \leq G$ [46]. Then, according to the constraints of (6), we get $q_n = v(\theta_1, r_1) + \sum_{j=1}^n \Delta_j$, $i \in \mathcal{G}$. As q_i always can be substituted by a function with variables $\{\theta_1, \ldots, \theta_i, r_1, \ldots, r_i\}$, $i \in \mathcal{G}$, we only use a symbol q_i here to represent the payment, but not any form of functions. By substituting this into the object function of (6), the function can be rewritten as

$$\max_{\{r_i, P_{ac,i}\}} U_{sta} = \sum_{i=1}^{G} (1 - P_{loss,i}) P_{ac,i} P_{r,i}$$
$$\cdot (v(\theta_1, r_1) + \sum_{j=1}^{i} \Delta_j - r_i \xi), \quad (7)$$

where the variable $\{q_i\}$ has been removed compared with (6). By rearranging (7), the optimization problem can be described as

$$\max_{\{r_{i}, P_{ac,i}\}} U_{sta} = \sum_{i=1}^{G} \{ (1 - P_{loss,i}) P_{ac,i} P_{r,i} (v(\theta_{i}, r_{i}) - r_{i}\xi) + (v(\theta_{i}, r_{i}) - v(\theta_{i+1}, r_{i})) \sum_{k=i+1}^{G} \times (1 - P_{loss,k}) P_{ac,k} P_{r,k} \},$$

s.t. C1 : $r_{\min} \le r_{1} \le r_{2} \le \ldots \le r_{G} \le r_{\max},$
C2 : $P_{loss,i} \le \varepsilon, \quad P_{ac,i} = \{0, 1\}, \ i \in \mathcal{G}.$ (8)

C. Optimal Contract Solution

To solve (8), we propose a two-step iterative algorithm. In the first step, given $\{P_{ac,i}\}$, we derive the optimal charging rates for each type denoted as $\{r_i^*\}$. In the second step, based on the $\{r_i^*\}$, we obtain the optimal $\{P_{ac,i}^*\}$. The algorithm converges under certain conditions, which will be discussed in the later part of this subsection.

1) Optimal Charging Rates: In the charging system, the waiting time of a newly arrived platoon may be affected by the service times of the EVs which are before it in the queue. As these EVs can belong to any type- θ , the charging rates of different types may impact the waiting time, and further may impact P_{loss} of platoons. Furthermore, due to the stochastic characteristics of the charging times of all types of platoons, the optimization of the charging rates is an NP-hard problem in terms of computational complexity. To solve the problem efficiently, we rewrite the objective function of (8) as $U_{sta}' = (1 - \varepsilon) \sum_{i=1}^{G} \{P_{ac,i} P_{r,i}(v(\theta_i, r_i) - r_i \xi) + (v(\theta_i, r_i) - v(\theta_{i+1}, r_i)) \sum_{k=i+1}^{G} P_{ac,k} P_{r,k}\}. \text{ As } 1 - P_{loss,i} \ge 1 - \varepsilon, i \in \mathcal{G},$ then $U'_{sta} \leq U_{sta}$. Thus we improve the utility of the charging station by optimizing its lower bound.

Let $H_i = P_{ac,i}P_{r,i}(v(\theta_i, r_i) - r_i\xi) + (v(\theta_i, r_i) - v(\theta_{i+1}, r_i))\sum_{k=i+1}^{G} P_{ac,k}P_{r,k}$. In the first step, given $\{P_{ac,i}\}$, the objective function can be expressed as $\max_{\{r_i\}} U'_{sta}$ = $(1 - \varepsilon) \sum_{i=1}^{G} H_i$. As H_i is only related to r_i , $\{r_i^*\}$ can be obtained by maximizing each H_i separately.

Lemma 1: If $P_{r,i} \ge \frac{(\theta_{i+1}^2 - \theta_i^2)}{\theta_i^2} \sum_{k=i+1}^G P_{r,k}$, H_i is a concave function on r_i , $1 \le i < G$. Proof: Let $A = \sum_{k=i+1}^G P_{ac,k} P_{r,k}$ and $B = P_{ac,i} P_{r,i}$.

Then the second derivative of H_i can be given as

$$d^{2}H_{i}/dr_{i}^{2} = -B\theta_{i}^{2}(1+\theta_{i+1}r_{i})^{2} + A(\theta_{i+1}^{2}-\theta_{i}^{2} + 2\theta_{i+1}^{2}\theta_{i}r_{i} - 2\theta_{i}^{2}\theta_{i+1}r_{i}).$$
(9)

It is clear that $B\theta_i^2(1+2\theta_{i+1}r_i) \leq B\theta_i^2(1+\theta_{i+1}r_i)^2$. Recall that $\begin{array}{l} \theta_{i+1} > \theta_i, \text{ we have } A(\theta_{i+1}^2 - \theta_i^2)(1 + 2\theta_{i+1}r_i) = A(\theta_{i+1}^2 - \theta_i^2 + 2\theta_{i+1}^3 r_i - 2\theta_i^2 \theta_{i+1}r_i) > A(\theta_{i+1}^2 - \theta_i^2 + 2\theta_{i+1}^2 \theta_i r_i - 2\theta_i^2 \theta_{i+1}r_i). \\ \text{According to the sufficient condition given in Lemma 1,} \end{array}$ $A(\theta_{i+1}^2 - \theta_i^2)(1 + 2\theta_{i+1}r_i) \le B\theta_i^2(1 + 2\theta_{i+1}r_i)$. By combining the above inequalities, we can prove $d^2H_i/dr_i^2 < 0$ which indicates H_i is a concave function on r_i .

It is worth noting that, if the concave condition in Lemma 1 is not satisfied, we can first solve the optimization problem (8) without the constraint $r_{min} \leq r_1 \leq r_2 \leq \ldots \leq r_G \leq r_{max}$ by Lagrangian relaxation. Then, we need to check whether the solution of the relaxed problem satisfies this constraint. In the following sections, we consider the case that $P_{r,i}$, $i \in \mathcal{G}$, satisfy the condition specified in Lemma 1. Thus, each \hat{r}_i which maximizes H_i can be obtained at the boundary points, i.e., 0 or r_{max} , or at the critical point by setting $dH_i/dr_i = 0$ according to Fermat's theorem. However, the obtained set $\{\hat{r}_i\}$ may not satisfy the first constraint in (8). The sub-sequences of the set which are not in the increasing order, are called infeasible sub-sequences.

As $\{H_i\}$ are concave functions, the infeasible sub-sequences can be replaced by feasible sub-sequences $\{r_i^*\}$ iteratively. The

algorithm is presented as follows [46].

a) Initialize: $\hat{r}_i = \arg \max_{\{r_i\}} H_i, i \in \mathcal{G}$.

b) Repeat: While there exists an infeasible sub-sequence ${\hat{r}_i, \hat{r}_{i+1}, \dots, \hat{r}_j}$, set $\hat{r}_k = \arg \max_{\{r\}} \sum_{s=i}^{J} H_s(q), k \in \{i, i+1\}$ $1, \ldots, j$.

c) Output: The optimal charging rates $\{r_i^*\} = \{\hat{r}_i\}$.

2) Optimal Admission Probabilities: Now, having obtained the charging rates $\{r_i^*\}$, we derive the optimal $\{P_{aci}^*\}$. Considering G types of charging rates in the charging station, i.e., $\{r_1^*, r_2^*, \ldots, r_G^*\}$, and the charging times are exponentially distributed with means $\{1/\mu_1, 1/\mu_2, \ldots, 1/\mu_G\}$, respectively. Let L be the number of EVs in the charging system when a new EV platoon arrives at the station. For the waiting time of a new platoon, there are two cases. The first one is L < c, where the waiting time for the new platoon equals to 0 due to the spare chargers. In the second case where L > c, the new platoon should wait L - c + 1 EVs having been served before starting its own service. Thus, the probability of the waiting time w can be expressed as

$$P_{w}(w \leq \zeta) = \begin{cases} 1, & 0 \leq L < c \\ \int_{0}^{\zeta} \frac{(c/\bar{t})^{L-c+1} x^{L-c}}{\Gamma(L-c+1)} e^{-cx/\bar{t}} dx, & L \geq c, \end{cases}$$
(10)

where $\Gamma(\hat{y}) = \int_0^\infty \hat{x}^{\hat{y}-1} e^{-\hat{x}} d\hat{x}$. \bar{t} is the average service time for a charger to finish charging one EV, which is given as

$$\bar{t} = \frac{\sum_{i=1}^{G} P_{ac,i} P_{r,i} / \mu_i}{\sum_{i=1}^{G} P_{ac,i} P_{r,i}}.$$
(11)

Based on (10), the service loss probability of type- θ_i platoons can be presented as

$$P_{loss,i} = P_w(w > T_{\theta,i}). \tag{12}$$

Recall that $T_{\theta,1} > T_{\theta,2} > \ldots > T_{\theta,G}$, which means if $P_{loss,i} \leq$ ε , then $P_{loss, i} < \varepsilon$, where j < i and $j \in \mathcal{G}$. Thus, we can obtain the optimal admission probabilities $\{P_{ac,i}^*\}$ by searching for the critical $P_{loss,k}$ which satisfies that $P_{loss,k} > \varepsilon$ and $P_{loss,k-1} \leq \varepsilon$. As the charging station is rational, $q_i - r_i \xi \geq 0$, then $\{P_{ac,i}^*\}$ is given as $\{P_{ac,1}^*=1, P_{ac,2}^*=1, \dots, P_{ac,k-1}^*=1, P_{ac,k}^*=0, \dots, P_{ac,G}^*=0\}$.

The complete optimal contract-based charging rate assignment and admission control are illustrated in Algorithm 1. The maximum number of iterations of Algorithm 1 is O(G+1).

Theorem 1: Under the concave condition stated in Lemma 1, Algorithm 1 converges monotonically to the optimal contract-based charging rate assignment and admission control policy.

Proof: Let us consider two iterations j and j + 1. Let $\{r_{i,i}^*\}$ and $\{r_{i,i+1}^*\}$, $i \in \mathcal{G}$, denote the optimal charging rates obtained from these two iterations, respectively. Furthermore, let G_i and G_{i+1} denote the highest type index of platoons admitted charging in the iteration j and j + 1, respectively.

Algorithm 1 The Optimal Charging Rate Assignment and Admission Control Schemes

Initialization: Let $P_{ac,i}^* = 1, i \in \mathcal{G}$.

- 1: Step 1: Based on the given $\{P_{ac,i}^*\}$, compute the optimal charging rates $\{r_i^*\}, i \in \mathcal{G}$;
- Step 2: According to the obtained {r_i*}, searching for the critical P_{loss,k};

3: if $P_{loss,k} == \emptyset$ then

- 4: Break;
- 5: **else**
- 6: Let $\{P_{ac,1}^* = 1, P_{ac,2}^* = 1, \dots, P_{ac,k-1}^* = 1, P_{ac,k}^* = 0, \dots, P_{ac,G}^* = 0\};$ 7: Set G = k - 1;8: Go to Step 1; 9: end if
- 10: **return** $\{r_i^*\}$ and $\{P_{ac,i}^*\}, i \in \mathcal{G}$.

Then, the first derivative of H_i of these two iterations can be expressed as following.

$$H'_{i,j} = dH_{i,j}/dr_i = P_{ac,i}P_{r,i}(\frac{\theta_i}{1+\theta_i r_i} - \xi) + (\frac{\theta_i}{1+\theta_i r_i} - \frac{\theta_{i+1}}{1+\theta_{i+1} r_i}) \sum_{k=i+1}^{G_j} P_{ac,k}P_{r,k}, \quad (13)$$

$$H'_{i,j+1} = dH_{i,j+1}/dr_i = P_{ac,i} P_{r,i} \left(\frac{\theta_i}{1+\theta_i r_i} - \xi\right) + \left(\frac{\theta_i}{1+\theta_i r_i} - \frac{\theta_{i+1}}{1+\theta_{i+1} r_i}\right) \sum_{k=i+1}^{G_{j+1}} P_{ac,k} P_{r,k}.$$
(14)

As both $H_{i,j}$ and $H_{i,j+1}$ are concave functions, the optimal rates $r_{i,j}^*$ and $r_{i,j+1}^*$ are obtained by setting $H'_{i,j} = 0$ and $H'_{i,j+1} = 0$, respectively. Let $H'_{i,j}(r_{i,j}^*)$ represent substituting $r_{i,j}^*$ into $H'_{i,j}$. To prove $r_{i,j}^* < r_{i,j+1}^*$ by contradiction, we assume $r_{i,j}^* \ge r_{i,j+1}^*$. Note that $\sum_{k=i+1}^{G_j} P_{ac,k} P_{r,k} >$ $\sum_{k=i+1}^{G_{j+1}} P_{ac,k} P_{r,k}$, due to $G_j > G_{j+1}$. If $r_{i,j}^* = r_{i,j+1}^*$, it is obvious that $H'_{i,j}(r_{i,j}^*) \ne H'_{i,j+1}(r_{i,j+1}^*)$, which contradicts with $H'_{i,j}(r_{i,j}^*) = H'_{i,j+1}(r_{i,j+1}^*) = 0$. If $r_{i,j}^* > r_{i,j+1}^*$, as $H_{i,j}$ is a concave function, $H'_{i,j}(r_{i,j+1}^*) > 0$. Comparing $H'_{i,j}(r_{i,j+1}^*)$ with $H'_{i,j+1}(r_{i,j+1}^*)$, due to the second term of $H'_{i,j}(r_{i,j+1}^*)$ being less than that of $H'_{i,j+1}(r_{i,j+1}^*)$, we can conclude that $H'_{i,j+1}(r_{i,j+1}^*) > H'_{i,j}(r_{i,j+1}^*) > 0$, which contradicts with $H'_{i,j}(r_{i,j}^*) = H'_{i,j+1}$. As the charging rates increase, the average charging time gets shorter which will in turn decrease the service loss probabilities. As a result, the algorithm will come to a convergence.

Under the condition that the number of EVs in the charging system is L, we have obtained the optimal charging rates and access control probabilities which are denoted as $\{r_i^*(L)\}$ and $\{P_{ac,i}^*(L)\}$, respectively. The optimal charging price $\{q_i^*(L)\}$ for platoons can be easily drawn based on $\{r_i^*(L)\}$. It should be noted that the value of L, which is affected by the platoon arrival rate, the size of platoon and the charging service policy, etc., will be analyzed in the next section.

V. STEADY-STATE DISTRIBUTION OF CHARGING SYSTEM

In this section, we will incorporate the proposed contractbased charging schemes into the queuing model, and obtain the steady-state distribution of the drawn equilibrium equations of the charging system, which will be used by the performance analysis of the proposed charging schemes.

A. Dynamics of Imported Renewable Energy

Let $f_1(b, s)$ denote the probability of the renewable energy imported at b units in time slot t + 1 conditioned by s EVs that have been served in the charging station during time slot t. According to (1), $f_1(b, s)$ can be derived as follows.

1) Case 1: If b = 0, which means no renewable energy will be imported in the charging station in time slot t + 1, this situation can be caused by two reasons. One is no EV has been charged during time slot t. The other is that there have been some EVs served in time slot t, but no renewable energy is generated in time slot t + 1. Thus, the probability of this case can be written as

$$f_1(b,s) = \begin{cases} 1, & b = 0, s = 0\\ P_e(e(t+1) = 0), & b = 0, s > 0. \end{cases}$$
(15)

2) Case 2: If 0 < b < M, which requires both the number of the served EVs in time slot t and the renewable energy generated in time slot t + 1 are no less than b, then we have

$$f_1(b,s) = \begin{cases} P_e(e(t+1) = b), & 0 < b < M, s > b \\ P_e(e(t+1) \ge b), & 0 < b < M, s = b \\ 0, & 0 < b < M, 0 < s < b. \end{cases}$$
(16)

3) Case 3: If b = M, i.e., both the number of the served EVs and the generated renewable energy should be no less than M, then we get

$$f_1(b,s) = \begin{cases} P_r(e(t+1) \ge M), & b = M, s \ge b\\ 0, & b = M, 0 < s < M. \end{cases}$$
(17)
4) Case 4: If $b < 0, b > M$ or $s < 0$, then $f_1(b,s) = 0$.

B. Dynamics of EVs in the Charging System

In this subsection, we study the dynamics of the number of EVs as well as the imported renewable energy in the charging system. Let P(n, i, m, b) be the probability of the charging station holding *i* EVs with *b* renewable energy imported at time slot t + 1 under the condition that it has *n* EVs with *m* units renewable electricity imported at time slot *t*. Recall that time-slot duration τ is short, and there is no more than one platoon arrival during one time slot. We denote the probability of *z* new EVs arrivals at the charging station during a time slot as

$$\beta_{z} = \begin{cases} e^{-\lambda_{p}\tau}, & z = 0\\ e^{-\lambda_{p}\tau}\lambda_{p}\tau \cdot P_{l,z}, & z > 0. \end{cases}$$
(18)

For each time slot *t*, the arriving time of each platoon is i.i.d. random variable. The probability of the time of the platoon arrival in the charging station at time $t + t_a$ given that the

platoon arrival has occurred, is a conditional probability, and can be expressed as

$$P_{arr}(t_a|\mathbf{A}) = \begin{cases} 1/\tau, & 0 \le t_a \le \tau\\ 0, & otherwise, \end{cases}$$
(19)

where A denotes the event of a platoon arrival.

With the above results, two cases are considered as follows.

1) Case 1: No new platoons join the charging system in time slot t. Since there is no EV joining, comparing the number of EVs at time slot t + 1 and t, we can find that n - i EVs have finished charging during time slot t. This case can be further divided into two scenarios.

a) Scenario 1: No platoon arrives during this time slot. The probability of this scenario can be denoted as

$$P_{1a}(n, i, m, b) = \beta_0 \cdot {\binom{\min\{c, n\}}{n-i}} (1 - e^{-\tau/\bar{t}_n})^{n-i} \cdot e^{-\tau(\min\{c, n\} - n+i)/\bar{t}_n} f_1(b, n-i), \quad (20)$$

where \bar{t}_n is the average charging time for an EV served by one charger according to the contract charging rates $\{r_i^*(n)\}$, given the condition that there are *n* EVs in the queuing system. \bar{t}_n can be obtained from (11).

b) Scenario 2: The second scenario is that a platoon arrives during time slot t, but it cannot join the charging system either due to the insufficient available capacity of the charging station or because of the admission control scheme. Given that there are n EVs in the charging system at the beginning of time slot t, we consider that a platoon arrives at the charging system at time $t\tau + t_a$. If there are v EVs at time $t\tau + t_a$, which means n - v EVs have been served in time $(t\tau, t\tau + t_a)$, and v - iEVs will be served during time $(t\tau + t_a, (t+1)\tau)$. Under these conditions, we can get the probability of the platoon getting admission as

$$P_{in}(t\tau + t_a) = \begin{cases} 0, & z > N - v \\ \sum_{x=1}^{G} P_{ac,x}^*(v) P_{r,x}, & z \le N - v. \end{cases}$$
(21)

The probability of the dynamics of the platoons in this scenario can be divided into two parts, namely P_{1b1} and P_{1b2} . P_{1b1} is the probability that the platoon cannot join the station due to the lack of available capacities. P_{1b2} is the probability that the leaving of the platoon is caused by the admission control policy. P_{1b1} and P_{1b2} are respectively expressed as follows.

$$P_{1b1} = f_1(b, n-i) \int_0^\tau P_{arr}(t_a|A) \sum_{v=n-\min\{n,c\}}^n \\ \times \sum_{k=N-v+1}^{Z_{\max}} \beta_k \cdot \mathbf{1}(0 \le v - i \le \min\{v,c\}) \\ \cdot f_2(n, n-v, t_a) f_2(v, v - i, \tau - t_a) dt_a.$$
(22)
$$P_{1k2} = f_1(b, n-i) \int_0^\tau P_{arr}(t_a|A) \sum_{v=1}^n p_{arr}(t_a|A) \sum_{v$$

$$\Gamma_{1b2} = f_1(b, n-t) \int_0^{\infty} \Gamma_{arr}(t_a|A) \sum_{v=n-\min\{n,c\}} \sum_{k=1}^{\min\{N-v, Z_{max}\}} \beta_k (1 - \sum_{x=1}^G P_{ac,x}^*(v) P_{r,x}) \\ \cdot \mathbf{1}(0 \le v - i \le \min\{v, c\}) f_2(n, n-v, t_a) \\ \cdot f_2(v, v - i, \tau - t_a) dt_a.$$
(23)

In (22) and (23), $\mathbf{1}(\hat{x})$ is an indicator function which equals 1 if \hat{x} is true and 0 otherwise. The function $f_2(w, s, \Delta t)$ denotes the probability that on average s EVs have been charged during time Δt , if there were w EVs at the beginning, which could be described as

$$f_2(w, s, \Delta t) = {\min\{c, w\} \choose s} (1 - e^{-\Delta t/\tilde{t}_w})^s \cdot e^{-\Delta t(\min\{c, w\} - s)/\tilde{t}_w}.$$
 (24)

The probability P(n, i, m, b) of this case can be stated as

$$P_{1}(n, i, m, b) = \begin{cases} P_{1a} + P_{1b1} + P_{1b2}, & (n-i) \in [0, \min\{c, n\}] \\ 0, & \text{otherwise.} \end{cases}$$
(25)

2) Case 2: In this case, one platoon arrives and joins the charging station during time slot t. Similar to the second scenario of Case 1, we assume that when the platoon consisting of k EVs arrives at the station at time $t+t_a$, there are v EVs in the charging system. Recall that there is a capacity limitation of the charging station, then $k + v \le N$ should be satisfied. As a result, n - v EVs have finished charging during time $(t\tau, t\tau + t_a)$, and i - (k+v) EVs will be fully charged during time $(t\tau + t_a, (t+1)\tau)$. The probability of this case can be expressed as

$$P_{2}(n, i, m, b) = \int_{0}^{\tau} P_{arr}(t_{a}|A) \sum_{k=1}^{\mathcal{K}} \beta_{k}$$

$$\cdot f_{1}(b, n+k-i) \sum_{v=\mathcal{V}_{1}}^{\mathcal{V}_{2}} (1 - \sum_{x=1}^{G} P_{ac,x}^{*}(v) P_{r,x})$$

$$\cdot \mathbf{1}(0 \le k + v - i \le \min\{k + v, c\})$$

$$\cdot f_{2}(n, n - v, t_{a}) f_{2}(k + v, k + v - i, \tau - t_{a}) dt_{a}, \quad (26)$$

where $\mathcal{K} = \min\{Z_{\max}, N-n+\min\{n, c\}\}, \mathcal{V}_1 = n-\min\{n, c\},$ and $\mathcal{V}_2 = \min\{n, N-l\}$. Based on (25) and (26), the probability P(n, i, m, b) can be denoted as

$$P(n, i, m, b) = P_1(n, i, m, b) + P_2(n, i, m, b),$$

$$0 \le n, i \le N, \quad 0 \le m, b \le M. \quad (27)$$

C. Steady-State Distribution

Now, we shall study the steady-state distribution of the EVs and the imported renewable energy in the charging system. Let p(i, b) denote the steady-state probability that the system is in state S = (i, b) where the charging station holds *i* EVs and the amount of the imported renewable energy is *b*. The steady-state equations are

$$p(i,b) = \sum_{n=0}^{N} \sum_{m=0}^{M} p(n,m) P(n,i,m,b),$$

$$0 \le i \le N, \quad 0 \le b \le M. \quad (28)$$

By solving a set of (N + 1)(M + 1) linear equations in (28), together with the normalization equation $\sum_{n=0}^{N} \sum_{m=0}^{M} p(n,m) = 1$, we can get the steady-state distributions of the charging system. As the corresponding embedded Markov chain is ergodic, the charging system has a unique steady-state solution [22].



Fig. 2. The relationship between the main system components.



Fig. 3. 69-bus distribution test system [47].

Based on the obtained steady-state probabilities, we can get some performance indicators of the charging system. For instance, the average EVs in the system and the average imported renewable energy can be given as $\bar{L} = \sum_{n=0}^{N} n \sum_{m=0}^{M} p(n,m)$, $\bar{r} = \sum_{m=0}^{M} m \sum_{n=0}^{N} p(n,m)$, respectively. According to these indicators, the optimal contracts in the steady-states are derived. Then, the effects of the contact-based scheme on both the utility maximization of the station and the adjustment of grid load level can be obtained. To introduce the main flow of our proposed charging schemes more clearly, we illustrate the relationship between the main system components in Fig. 2.

VI. NUMERICAL RESULTS

In this section, we evaluate the performance of the proposed schemes through simulation on the IEEE 69-bus distribution test system as shown in Fig. 3, where the topology of the grid as well as typical parameters of lines and devices are set according to [48]. In the test system, each bus belongs to a district which is randomly categorized into a residential, commercial or industrial district. According to electricity consumption profiles of various districts, base load of each district is added to transformers that connect districts to the grid [47]. As platoons are often used for industrial transportation, we consider the charging stations located in the industrial districts. We add the charging stations and the renewable energy generators into industrial districts, and connect them to the corresponding transformers. The renewable energy is generated by photovoltaic panels equipped in the stations. We adopt the climate data set of Seattle [49]. Each charging station is considered to have N = 7 parking lots and c = 4 chargers. The duration of each time slot τ is assumed to be 1 minute. The maximal size of each platoon is $Z_{max} = 5$ and the arrival rate of EV platoons is set



Fig. 4. Load level of district S1 with different rate assignment schemes.



Fig. 5. Load level of branch S2 with different rate assignment schemes.

 $\lambda_p = 1/10$ platoon/minute. According to the requirement of charging rates, these platoons are classified into five categories with $\theta = \{1.0, 1.2, 1.5, 1.8, 2.0\}$, respectively. The charging QoS threshold ε is 0.1.

In practice, each district is served by a substation equipped with transformers, which requires the total demand of the customers belonging to the district under the nominal capacities of the transformers. In Fig. 4, we show the impact of different charging rate assignment schemes on the demand load of the transformers in the industrial district S1. The fixed rate scheme delivers 14.4 kW of electricity to the EVs constantly, which is specified as the level 2 of EV charging in the U.S. National Electric Code (NEC). The other two schemes are the Contract-Based (CB) rate assignment with incorporated Renewable Energy (RE) source and without it, respectively. As shown in Fig. 4, significant overloads are experienced from 8:00-11:00 with the fixed charging rate. In contrast, both the two CB rate assignments can effectively moderate the stress of the electricity demand under the capacity of the transformer during the peak hours. Especially the CB rate with RE, which reduces approximately 20% of the load level compared with the fixed rate scheme when the solar generator equipped in the charging station could create adequate power at noon time. Furthermore, the two CB schemes achieve a good valley-filling effect in the grid, which improves the energy utilization.

Fig. 5 indicates the load level performance of S2 which reflects the performance of these schemes on the branch of the 69-bus system. The load level of this branch is different from that of district S1, as the branch consists of different types of districts, and each type has distinct load profiles.



Fig. 6. Electricity price of the charging station without renewable energy.



Fig. 7. Utility of the charging station with different schemes.

These mixed characteristics of the load profiles may undermine the effectiveness of the load level adjustment given by the proposed scheme. For example, the load level of this branch is close to 97% at 12:00 adopting the CB scheme without RE. However, it could be reduced to 91% by applying the CB scheme with RE, which shows the effect of the renewable energy in peak load shaving.

Fig. 6 and Fig. 7 show the electricity price and the utility of the charging station which is located in *S*1 and has no renewable energy, respectively. The electricity price depends on the load level of the power grid. As the grid is the main power source of the charging station, the three charging schemes in Fig. 7 have the identical charging cost at a given time.

By comparing Fig. 6 and Fig. 7, we get the following observations. The utility plot of the fixed rate scheme has a similar shape as the charging cost. The reason is that the charging rate is 14.4kW and the price is fixed under a given grid load level. In the variable rate scheme, the charging price is proportional to the rate chosen by a platoon, and the scaling factor depends on the grid load. Given a scaling factor, each platoon determines the optimal charging rate that mostly benefits itself. A platoon chooses high rate when the price is low, and vice versa. Thus, the utility gained by this scheme has a flat shape. From Fig. 7, it is clear that our proposed CB scheme yields higher profit to the station compared to other schemes, especially in the valley load time. The reason is that the CB scheme can raise the charging price to make LDIC binding. Thus, compared to the other schemes which cannot



Fig. 8. Comparison of the optimal utility of (8) with its lower bound.



Fig. 9. Average service loss probabilities with different schemes.

adjust the price according to the type of platoon, our scheme makes part of the charging utilities transfer from the platoons to the station. The less electricity cost at the valley load time, the greater the gap between the contract-based charging price and the actual electricity cost. Therefore, larger profits can be obtained by the station. The characteristics of the CB scheme make the shape of the utility plot roughly opposite to the shape of the charging cost curve shown in Fig. 6. It should be noted that for a given time, the increase in the charging price in our proposed algorithm is on the electricity cost at that moment. Compared to the charging price at daytime, the resulting charging price at night is still lower. Thus, the rational platoons still prefer to be charged at night.

Fig. 8 illustrates the comparison of the optimal utility of problem (8) with the lower bound of the utility obtained from the relaxed optimization problem. In the relaxed problem, we replace $1 - P_{loss,i}$ ($i \in \mathcal{G}$) with $1 - \varepsilon$. Since the charging station is modeled as a complicated stochastic queuing system, the steady-state probabilities cannot be obtained explicitly. Thus, we cannot qualify the tightness of this relaxation through any mathematical expressions. However, we illustrate the quality of this bound with different power grid load levels through simulation as shown in Fig. 8. The average difference between the optimal utility and its lower bound is 5.9%.

We compare the impacts of the three schemes on the service loss probabilities with different load levels in Fig. 9. Due to information asymmetry, it is hard to distinguish the types of the platoons by applying the first two schemes. Accordingly, it is hard to implement any efficient admission



Fig. 10. Charging rates for different types of EV platoons with various load level of grid.



Fig. 11. Average waiting time of EV platoons in the charging station.

control strategies by these schemes. However, this shortcoming can be overcome by our proposed CB scheme, which adjusts the admission control policies according to the characteristics of different types of platoons together with the electricity cost. It is worth noting that by using the CB scheme the loss probability decreases at the point where the grid load level is 60%. This is caused by the adjustment of the contract-based admission policy where the highest type- θ platoons are driven to leave the charging station due to their profit-driven characteristics.

Fig. 10 shows the charging rates for different types of EV platoons with various load levels of the grid. With the increase of load level, all the rates decrease to make both the charging power consumption to better match power supply and the grid operates smoothly. It is noteworthy that when the load level increases to 60% and 70%, the charging rates of type-5, 4 and 3 platoons become zero, respectively. This is caused by our proposed charging admission control strategies. As charging rates decrease, the charging time for platoons becomes longer. To guarantee charging QoS requirements, the platoons with low tolerance to waiting time are not allowed to be charged in the station, and their corresponding charging service is suspended.

Fig. 11 gives the average waiting time of EV platoons in the charging station. Applying our proposed admission control strategies in platoon charging scheduling, the average waiting time can be greatly reduced when the load level is above 50%. The reason is that some delay sensitive platoons are



Fig. 12. Average charging time of EVs belonging to various types of platoons.

not allowed to be charged in the station when the load level reaches 60%, which is shown in Fig. 1. Due to the reduced arrival rates of the platoons, the waiting time also decreases.

Fig. 12 shows the average charging time of EVs belonging to various types of platoons. It can be found that the type of platoons with less tolerance on waiting time has shorter average charging time. It is worth noting that there is no charging time record for type-3 platoons when the load level is above 60% and for type-4, 5 platoons when the load level is above 50%. Due to the charging admission control schemes, the station never provides charging service to the platoons in these cases.

VII. CONCLUSION AND FUTURE WORK

In this paper, we have proposed a queuing-based network model for studying EV platoons charging process. We first design the contract-based charging rate assignment and admission control schemes. Then, we incorporate the schemes into the queuing system and derive its steady-state probabilities. Through simulations, we have demonstrated that the proposed schemes result in the optimal utility for the charging station, while respecting the charging QoS requirements. Furthermore, the schemes greatly improve the regulation of the grid's peaks and valleys. The analytical results prove the validity of the queuing model and the contract-based scheme for the design and control of the charging stations.

As well as our proposed contract-based charging schemes, there are further ways to enhance the charging of EV platoons, which can be covered in future work. One possible research direction is ensuring the fairness of various types of EV platoons served in capacity-constrained charging stations. Furthermore, in charging stations with large parking areas, alternatives to FIFO charging policy can be deployed. The challenge is how to propose an incentive mechanism that improves charging efficiency through the order adjustment of queuing platoons. In addition, the design of cooperative platoon charging schemes among multi-stations is still an unexplored problem. In the case where some EVs with plenty of energy in their batteries, they could potentially act as energy sources instead of being energy consumers, incentive-driven vehicle-to-vehicle charging mechanism is also an interesting topic for future study.

REFERENCES

- C. Luo, Y.-F. Huang, and V. Gupta, "Placement of EV charging stations—Balancing benefits among multiple entities," *IEEE Trans. Smart Grid*, vol. 8, no. 2, pp. 759–768, Mar. 2017.
- [2] M. Saeednia and M. Menendez, "A consensus-based algorithm for truck platooning," *IEEE Trans. Intell. Transp. Syst.*, vol. 18, no. 2, pp. 404–415, Feb. 2017.
- [3] C. Shao, S. Leng, Y. Zhang, A. Vinel, and M. Jonsson, "Performance analysis of connectivity probability and connectivity-aware MAC protocol design for platoon-based VANETs," *IEEE Trans. Veh. Technol.*, vol. 64, no. 12, pp. 5596–5609, Dec. 2015.
- [4] J. Hu, G. Yang, H. W. Bindner, and Y. Xue, "Application of network-constrained transactive control to electric vehicle charging for secure grid operation," *IEEE Trans. Sustain. Energy*, vol. 8, no. 2, pp. 505–515, Apr. 2017.
- [5] P. Bolton and M. Dewatripont, *Contract Theory*. Cambridge, MA, USA: MIT Press, 2005, pp. 31–64.
- [6] E. Chan, "SARTRE automated platooning vehicles," in Proc. Transport Res. Arena, Apr. 2014.
- [7] X.-Y. Lu and S. E. Shladover, "Automated truck platoon control and field test," in *Road Vehicle Automation*. Springer, Jun. 2014, pp. 247–261.
- [8] Y. Choi, D. Kang, S. Lee, and Y. Kim, "The autonomous platoon driving system of the on line electric vehicle," in *Proc. ICCAS-SICE*, Aug. 2009, pp. 3423–3426.
- [9] K. Yu *et al.*, "Model predictive control for hybrid electric vehicle platooning using slope information," *IEEE Trans. Intell. Transp. Syst.*, vol. 17, no. 7, pp. 1894–1909, Jul. 2016.
- [10] Q. Wang, X. Liu, J. Du, and F. Kong, "Smart charging for electric vehicles: A survey from the algorithmic perspective," *IEEE Commun. Surveys Tuts.*, vol. 18, no. 2, pp. 1500–1517, 2nd Quart., 2016.
- [11] D. Tang and P. Wang, "Probabilistic modeling of nodal charging demand based on spatial-temporal dynamics of moving electric vehicles," *IEEE Trans. Smart Grid*, vol. 7, no. 2, pp. 627–636, Mar. 2016.
- [12] W. Tang and Y. J. Zhang, "A model predictive control approach for low-complexity electric vehicle charging scheduling: Optimality and scalability," *IEEE Trans. Power Syst.*, vol. 32, no. 2, pp. 1050–1063, Mar. 2017.
- [13] C. Shao, X. Wang, X. Wang, C. Du, and B. Wang, "Hierarchical charge control of large populations of EVs," *IEEE Trans. Smart Grid*, vol. 7, no. 2, pp. 1147–1155, Mar. 2016.
- [14] L. He, J. Yang, J. Yan, Y. Tang, and H. He, "A bi-layer optimization based temporal and spatial scheduling for large-scale electric vehicles," *Appl. Energy*, vol. 168, pp. 179–192, Apr. 2016.
- [15] M. Alonso, H. Amaris, J. G. Germain, and J. M. Galan, "Optimal charging scheduling of electric vehicles in smart grids by heuristic algorithms," *Energies*, vol. 7, no. 4, pp. 2449–2475, Apr. 2014.
- [16] J. Tan and L. Wang, "Real-time charging navigation of electric vehicles to fast charging stations: A hierarchical game approach," *IEEE Trans. Smart Grid*, vol. 8, no. 2, pp. 846–856, Mar. 2017.
- [17] W. Saad, Z. Han, H. V. Poor, and T. Basar, "Game-theoretic methods for the smart grid: An overview of microgrid systems, demand-side management, and smart grid communications," *IEEE Signal Process. Mag.*, vol. 29, no. 5, pp. 86–105, Sep. 2012.
- [18] E. S. Rigas, S. D. Ramchurn, and N. Bassiliades, "Managing electric vehicles in the smart grid using artificial intelligence: A survey," *IEEE Trans. Intell. Transp. Syst.*, vol. 16, no. 4, pp. 1619–1635, Aug. 2015.
- [19] A. Y. S. Lam, K.-C. Leung, and V. O. K. Li, "Capacity estimation for vehicle-to-grid frequency regulation services with smart charging mechanism," *IEEE Trans. Smart Grid*, vol. 7, no. 1, pp. 156–166, Jan. 2016.
- [20] X. Dong, Y. Mu, H. Jia, J. Wu, and X. Yu, "Planning of fast EV charging stations on a round freeway," *IEEE Trans. Sustain. Energy*, vol. 7, no. 4, pp. 1452–1461, Oct. 2016.
- [21] W. Alharbi and K. Bhattacharya, "Electric vehicle charging facility as a smart energy microhub," *IEEE Trans. Sustain. Energy*, vol. 8, no. 2, pp. 616–628, Apr. 2017.
 [22] X. Tan, B. Sun, and D. H. K. Tsang, "Queueing network models for
- [22] X. Tan, B. Sun, and D. H. K. Tsang, "Queueing network models for electric vehicle charging station with battery swapping," in *Proc. IEEE SmartGridComm*, Nov. 2014, pp. 1–6.
- [23] B. Sun, X. Tan, and D. H. K. Tsang, "Optimal charging operation of battery swapping stations with QoS guarantee," in *Proc. IEEE Int. Conf. Smart Grid Commun. (SmartGridComm)*, Nov. 2014, pp. 13–18.
- [24] P. Fan, B. Sainbayar, and S. Ren, "Operation analysis of fast charging stations with energy demand control of electric vehicles," *IEEE Trans. Smart Grid*, vol. 6, no. 4, pp. 1819–1826, Jul. 2015.

- [25] M. Zeng, S. Leng, S. Maharjan, S. Gjessing, and J. He, "An incentivized auction-based group-selling approach for demand response management in V2G systems," *IEEE Trans. Ind. Informat.*, vol. 11, no. 6, pp. 1554–1563, Dec. 2015.
- [26] E. Bitar and Y. Xu, "Deadline differentiated pricing of deferrable electric loads," *IEEE Trans. Smart Grid*, vol. 8, no. 1, pp. 13–25, Jan. 2017.
- [27] W. Shuai, P. Maillé, and A. Pelov, "Charging electric vehicles in the smart city: A survey of economy-driven approaches," *IEEE Trans. Intell. Transp. Syst.*, vol. 17, no. 8, pp. 2089–2106, Aug. 2016.
- [28] L. Duan, L. Gao, and J. Huang, "Cooperative spectrum sharing: A contract-based approach," *IEEE Trans. Mobile Comput.*, vol. 13, no. 1, pp. 174–187, Jan. 2014.
- [29] Z. Hasan and V. K. Bhargava, "Relay selection for OFDM wireless systems under asymmetric information: A contract-theory based approach," *IEEE Trans. Wireless Commun.*, vol. 12, no. 8, pp. 3824–3837, Aug. 2013.
- [30] M. Peng, X. Xie, Q. Hu, J. Zhang, and H. V. Poor, "Contract-based interference coordination in heterogeneous cloud radio access networks," *IEEE J. Sel. Areas Commun.*, vol. 33, no. 6, pp. 1140–1153, Jun. 2015.
- [31] A. Asheralieva and Y. Miyanaga, "Optimal contract design for joint user association and intercell interference mitigation in heterogeneous LTE-A networks with asymmetric information," *IEEE Trans. Veh. Technol.*, vol. 66, no. 6, pp. 5284–5300, Jun. 2017.
- [32] Y. Gao, Y. Chen, C.-Y. Wang, and K. J. R. Liu, "A contract-based approach for ancillary services in V2G networks: Optimality and learning," in *Proc. IEEE INFOCOM*, Apr. 2013, pp. 1151–1159.
- [33] T. Namerikawa, N. Okubo, R. Sato, Y. Okawa, and M. Ono, "Realtime pricing mechanism for electricity market with built-in incentive for participation," *IEEE Trans. Smart Grid*, vol. 6, no. 6, pp. 2714–2724, Nov. 2015.
- [34] K. Zhang et al., "Optimal energy exchange schemes in smart grid networks: A contract theoretic approach," in Proc. IEEE/CIC Int. Conf. Commun. China (ICCC), Jul. 2016, pp. 1–6.
- [35] Y. Xu, F. Pan, and L. Tong, "Dynamic scheduling for charging electric vehicles: A priority rule," *IEEE Trans. Autom. Control*, vol. 61, no. 12, pp. 4094–4099, Dec. 2016.
- [36] Z. Yu, S. Chen, and L. Tong, "An intelligent energy management system for large-scale charging of electric vehicles," *J. Power Energy Syst.*, vol. 2, no. 1, pp. 47–53, Mar. 2016.
- [37] P. You, Z. Yang, M.-Y. Chow, and Y. Sun, "Optimal cooperative charging strategy for a smart charging station of electric vehicles," *IEEE Trans. Power Syst.*, vol. 31, no. 4, pp. 2946–2956, Jul. 2016.
- [38] Y. Zhou, D. Yau, P. You, and P. Cheng, "Optimal-cost scheduling of electrical vehicle charging under uncertainty," *IEEE Trans. Smart Grid*, to be published.
- [39] A. Schuhl, "The probability theory applied to distribution of vehicles on two-lane highways," Eno Found. Highway Traffic Control, Washington, DC, USA, Tech. Rep., 1955, pp. 59–75.
- [40] Z. Fan, "A distributed demand response algorithm and its application to PHEV charging in smart grids," *IEEE Trans. Smart Grid*, vol. 3, no. 3, pp. 1280–1290, Sep. 2012.
- [41] J. Baz, Financial Derivatives: Pricing, Applications, and Mathematics. Cambridge, U.K.: Cambridge Univ. Press, 2004.
- [42] P. L. Vo, N. H. Tran, C. S. Hong, and S. Lee, "Network utility maximisation framework with multiclass traffic," *IET Netw.*, vol. 2, no. 3, pp. 152–161, Sep. 2013.
- [43] D. T. Ngo, L. B. Le, and T. Le-Ngoc, "Distributed Pareto-optimal power control for utility maximization in femtocell networks," *IEEE Trans. Wireless Commun.*, vol. 11, no. 10, pp. 3434–3446, Oct. 2012.
- [44] V. A. Babin, "Portfolio rules with log consumption utility and Cox-Ingersoll-Ross interest rate," *Comput. Math. Model.*, vol. 26, no. 2, pp. 175–183, Apr. 2015.
- [45] J. Medina, N. Müller, and I. Roytelman, "Demand response and distribution grid operations: Opportunities and challenges," *IEEE Trans. Smart Grid*, vol. 1, no. 2, pp. 193–198, Sep. 2010.
- [46] L. Gao, X. Wang, Y. Xu, and Q. Zhang, "Spectrum trading in cognitive radio networks: A contract-theoretic modeling approach," *IEEE J. Sel. Areas Commun.*, vol. 29, no. 4, pp. 843–855, Apr. 2011.
- [47] R. Yu, W. Zhong, S. Xie, C. Yuen, S. Gjessing, and Y. Zhang, "Balancing power demand through EV mobility in vehicle-to-grid mobile energy networks," *IEEE Trans. Ind. Informat.*, vol. 12, no. 1, pp. 79–90, Feb. 2016.
- [48] M. E. Baran and F. F. Wu, "Optimal capacitor placement on radial distribution systems," *IEEE Trans. Power Del.*, vol. 4, no. 1, pp. 725–734, Jan. 1989.
- [49] Climate Data Set of US Cities. Accessed: May 2009. [Online]. Available: http://sourceforge.net/p/gridlab-d/code/HEAD/tree/ data/US/tmy



Ke Zhang received the Ph.D. degree from University of Electronic Science and Technology of China in 2017. He is currently a Lecturer with the School of Information and Communication Engineering, University of Electronic Science and Technology of China. His research interests include scheduling of mobile edge computing, design and optimization of next-generation wireless networks, smart grid, and the Internet of Things.



Stein Gjessing (M'07) received the Dr. Philos. degree from University of Oslo in 1985. He is currently a Professor of computer science with the Department of Informatics, University of Oslo, His original work was in the field object oriented concurrent programming. He has been involved with the computer interconnects [Scalable Coherent Interface (IEEE Std. 1596)] and LAN/MANs [Resilient Packet Ring (IEEE Std. 802.17)]. His main research interests are currently network and transport protocols, network resilience, cognitive radio networks, vehicular networks, and the smart grid.



Yuming Mao is currently a Professor with the School of Information and Communication Engineering, University of Electronic Science and Technology of China, Chengdu, China, where he is also the Chair of the Department of Network Engineering. His main research interests include broadband communication networks, network organization and protocol analysis, transmission control protocol/Internet Protocol technology, network management and protocol, routing protocol, and network engineering. He received several awards, including

the first-grade, second-grade, and third-grade awards of the Ministry of Electronic Industry for science and technology progress and the second-grade national award for science and technology progress.



Supeng Leng (M'06) is currently a Professor with the School of Information and Communication Engineering, University of Electronic Science and Technology of China, Chengdu, China. He has been a Research Fellow with the Network Technology Research Center. He has published over 100 research papers. His research interests include resources, spectrum, energy, routing, and networking in broadband wireless access networks, vehicular networks, the Internet of Things, next-generation mobile networks, and smart grids. He serves as an organizing

committee chair and a technical program committee member for many international conferences as well as a reviewer for over 10 international research journals.



Yejun He (SM'09) received the Ph.D. degree in information and communication engineering from Huazhong University of Science and Technology in 2005. He is currently a Full Professor with the College of Information Engineering, Shenzhen University, China, where he is also the Director of Guangdong Engineering Research Center of Base Station Antennas and Propagation and the Shenzhen Key Laboratory of Antennas and Propagation. His research interests include wireless mobile communication and antennas and radio frequency. He is a fellow of IET. He is currently the IEEE Antennas and Propagation Society

Shenzhen Chapter Chair.



Sabita Maharjan (M'09) received the Ph.D. degree in networks and distributed systems from the Simula Research Laboratory, University of Oslo, Norway, in 2013. She is currently a Senior Research Scientist with the Simula Metropolitan Center for Digital Engineering, Norway, and an Associate Professor with the University of Oslo. Her current research interests include wireless networks, network security and resilience, smart grid communications, the Internet of Things, machine-to-machine communications, software-defined wireless networking, and the Internet of Vehicles.



Yan Zhang (M'05-SM'10) received the Ph.D. degree from the School of Electrical & Electronics Engineering, Nanyang Technological University, Singapore. He is currently a Full Professor with the Department of Informatics. University of Oslo, Norway. His current research interests include nextgeneration wireless networks leading to 5G, and green and secure cyber-physical systems (e.g., smart grid, healthcare, and transport). He is a Senior Member of the IEEE ComSoc, IEEE CS, IEEE PES, and IEEE VT societies. He serves as a TPC member for

numerous international conference, including IEEE INFOCOM, IEEE ICC, IEEE GLOBECOM, and IEEE WCNC. He is an Associate Technical Editor of IEEE Communications Magazine, an Editor of IEEE Network Magazine, IEEE TRANSACTIONS ON GREEN COMMUNICATIONS AND NETWORKING, IEEE COMMUNICATIONS SURVEYS & TUTORIALS, IEEE INTERNET OF THINGS JOURNAL, IEEE Vehicular Technology Magazine, and an Associate Editor of IEEE ACCESS. He serves as the Chair in a number of conferences. including IEEE CloudCom 2015, IEEE SmartGridComm 2015, IEEE PIMRC 2016, IEEE CloudCom 2016, IEEE ICCC 2016, IEEE CCNC 2016, IEEE GLOBECOM 2017, and IEEE VTC-Spring 2017. He is the IEEE Vehicular Technology Society Distinguished Lecturer.



Danny H. K. Tsang (M'82-SM'00-F'12) received the Ph.D. degree in electrical engineering from the Moore School of Electrical Engineering, University of Pennsylvania, USA, in 1989. During his leave from HKUST from 2000 to 2001, he assumed the role of Principal Architect at Sycamore Networks in the United States. Since 1992, he has been with the Department of Electronic & Computer Engineering, The Hong Kong University of Science and Technology, where he is currently a Professor. His current research interests include cloud computing, cognitive

radio networks, and smart grids. He was nominated to become an IEEE Fellow in 2012 and an HKIE Fellow in 2013. He was responsible for the network architecture design of the Ethernet MAN/WAN over SONET/DWDM networks. He invented the 64B/65B encoding (U.S. Patent US 6,952,405 B2) and contributed it to the proposal for the Transparent GFP in the T1X1.5 Standard that was advanced to become the ITU G.GFP Standard. The coding scheme has now been adopted by the International Telecommunication Union (ITU)'s Generic Framing Procedure recommendation GFP-T (ITU-T G.7041/Y.1303) and the Interfaces for the Optical Transport Network (ITU-T G.709). He was a Guest Editor of IEEE JOURNAL ON SELECTED AREAS IN COMMUNICA-TIONS' special issue on Advances in P2P Streaming Systems, an Associate Editor of Journal of Optical Networking (Optical Society of America), and a Guest Editor of IEEE SYSTEMS JOURNAL. He currently serves as a Technical Editor for IEEE Communications Magazine.